

Exercise: Instabilities in Dynamic Fields

The neural field dynamics of Amari are based on this equation:

$$\tau_u \dot{u}(x, t) = -u(x, t) + h_u + S(x, t) + \int dx' w(x - x') \sigma(u(x'))$$

The sigmoidal function is given by

$$\sigma(u) = \frac{1}{1 + \exp[-\beta_u u]}.$$

The interaction kernel is given by

$$w(x - x') = -c_{\text{inh}} + c_{\text{exc}} \exp \left[-\frac{(x - x')^2}{2\sigma_{\text{exc}}^2} \right].$$

Input localized around locations, x_i , of strength, S_i , and widths, σ_i is supplied in the form

$$S(x, t) = \sum_i S_i \exp \left[-\frac{(x - x_i)^2}{2\sigma_i^2} \right].$$

Use the interactive simulator `interactiveSim11.m` to reproduce the instabilities we discussed in the lecture.

1. Detection instability and reverse detection: increase localized input strength, S_i and then decrease it again.
2. Selection: Provide two localized inputs and vary their relative strength. Observe stabilization of a selection decisions.
3. Boost induced detection: Supply small subthreshold input and increase resting level.
4. Selection of categorical response: Provide two localized inputs of identical strength below threshold. Increase resting level. Vary noise to see how either category is selected.
5. Memory instability: vary resting level and probe if self-stabilized peaks are sustained.